

Figure 6-1 Comparison of the frequency magnitude responses of a 19-tap low-pass FIR filter and a 4th-order lowpass IIR filter.

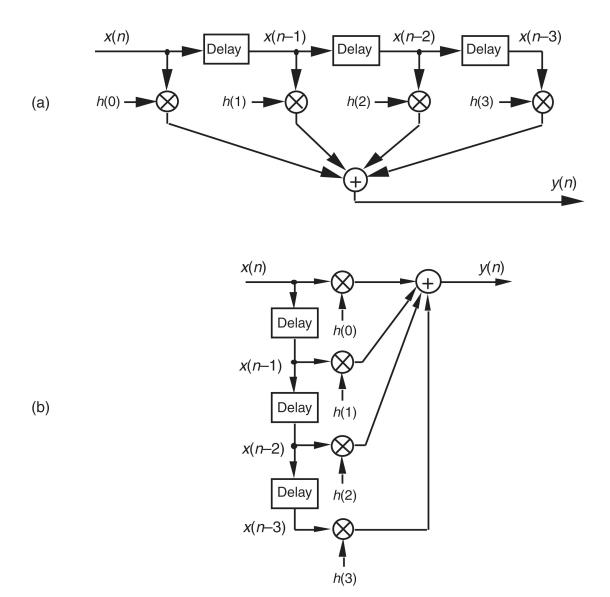


Figure 6-2 FIR digital filter structures: (a) traditional FIR filter structure; (b) rearranged, but equivalent, FIR filter structure.

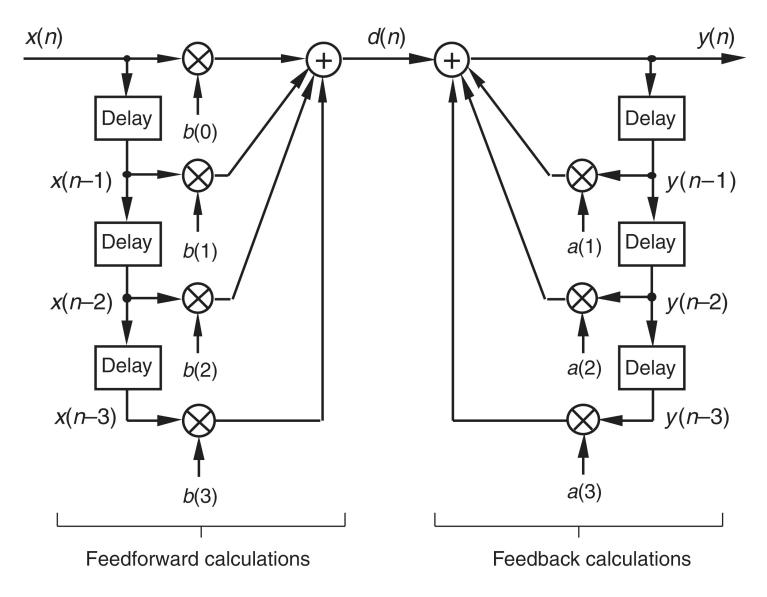
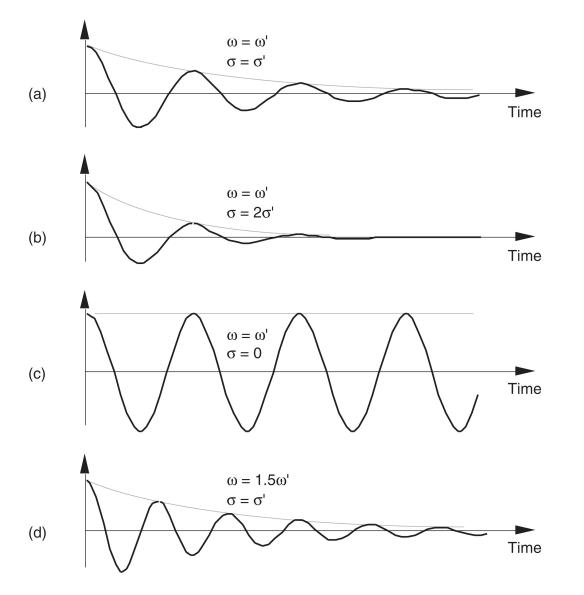


Figure 6-3 IIR digital filter structure showing feedforward and feedback calculations.



**Figure 6-4** Real part (cosine) of various  $e^{-st}$  functions, where  $s = \sigma + j\omega$ , to be correlated with f(t).

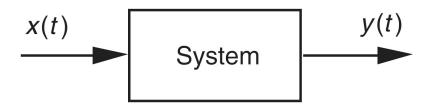
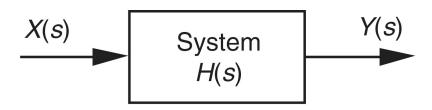
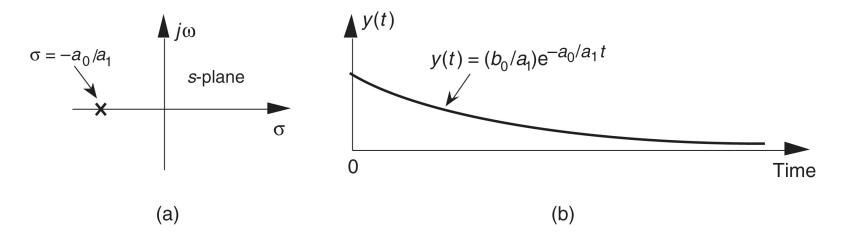


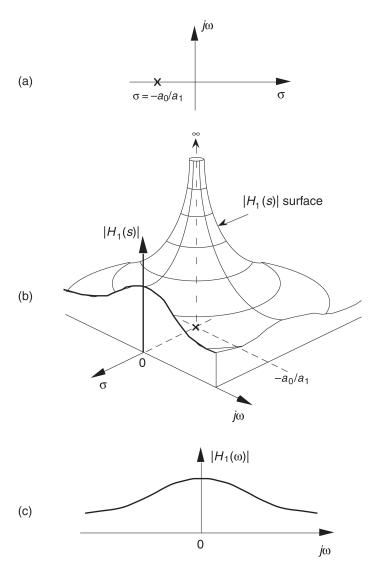
Figure 6-5 System described by Eq. (6-6). The system's input and output are the continuous-time functions x(t) and y(t) respectively.



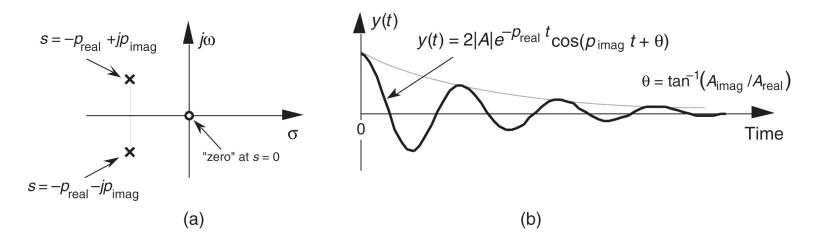
**Figure 6-6** Linear system described by Eqs. (6–10) and (6–11). The system's input is the Laplace function X(s), its output is the Laplace function Y(s), and the system transfer function is H(s).



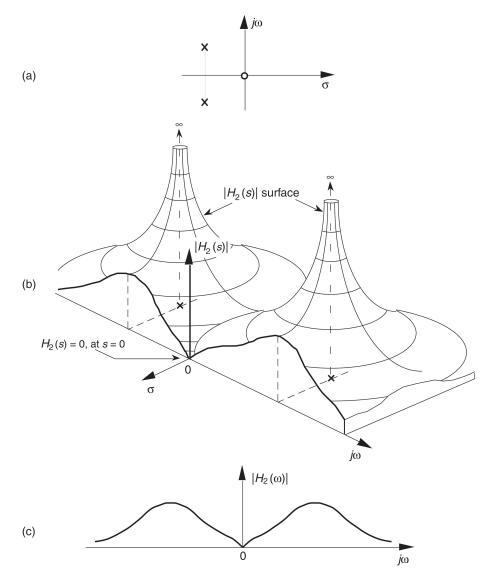
**Figure 6-7** Descriptions of  $H_1(s)$ : (a) pole located at  $s = \sigma + j\omega = -a_0/a_1 + j0$  on the s-plane; (b) time-domain y(t) impulse response of the system.



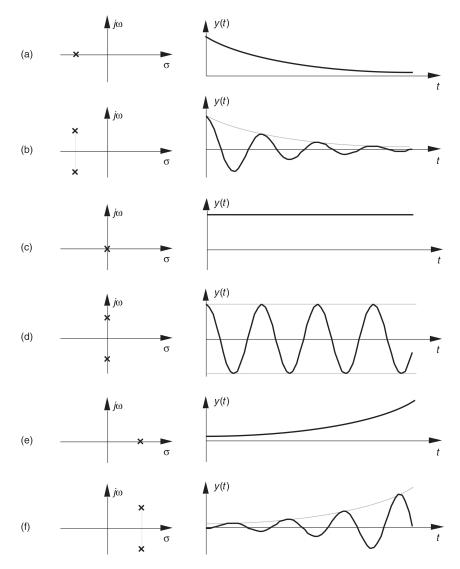
**Figure 6-8** Further depictions of  $H_1(s)$ : (a) pole located at  $\sigma = -a_0/a_1$  on the s-plane; (b)  $|H_1(s)|$  surface; (c) curve showing the intersection of the  $|H_1(s)|$  surface and the vertical  $\sigma = 0$  plane. This is the conventional depiction of the  $|H_1(\omega)|$  frequency magnitude response.



**Figure 6-9** Descriptions of  $H_2(s)$ : (a) poles located at  $s = p_{real} \pm jp_{imag}$  on the s-plane; (b) time-domain y(t) impulse response of the system.



**Figure 6-10** Further depictions of  $H_2(s)$ : (a) poles and zero locations on the s-plane; (b)  $|H_2(s)|$  surface; (c)  $|H_2(\omega)|$  frequency magnitude response curve.



**Figure 6-11** Various H(s) pole locations and their time-domain impulse responses: (a) single pole at  $\sigma < 0$ ; (b) conjugate poles at  $\sigma < 0$ ; (c) single pole located at  $\sigma = 0$ ; (d) conjugate poles located at  $\sigma = 0$ ; (e) single pole at  $\sigma > 0$ ; (f) conjugate poles at  $\sigma > 0$ .

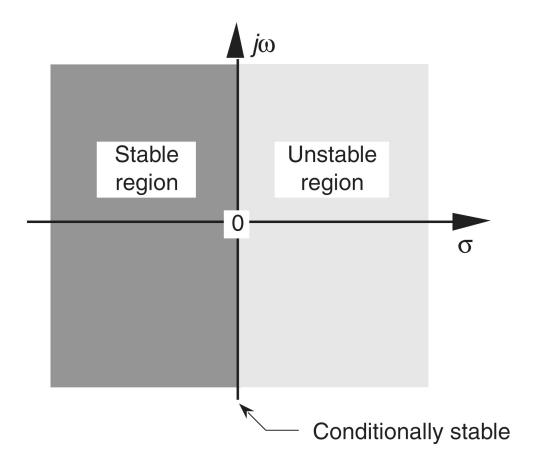
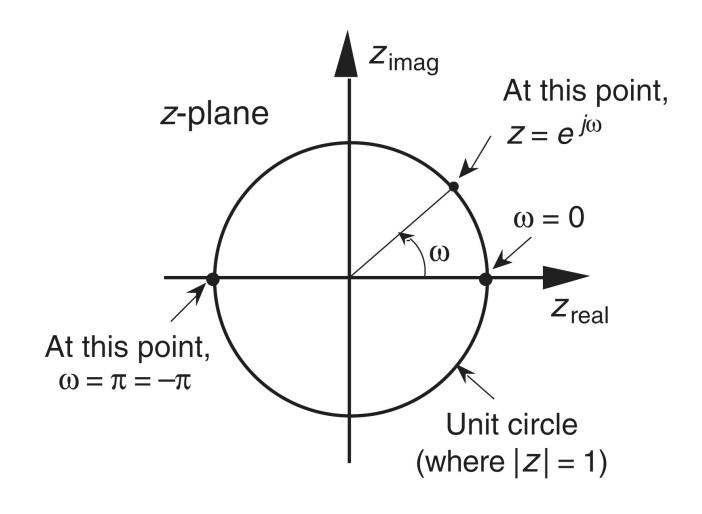
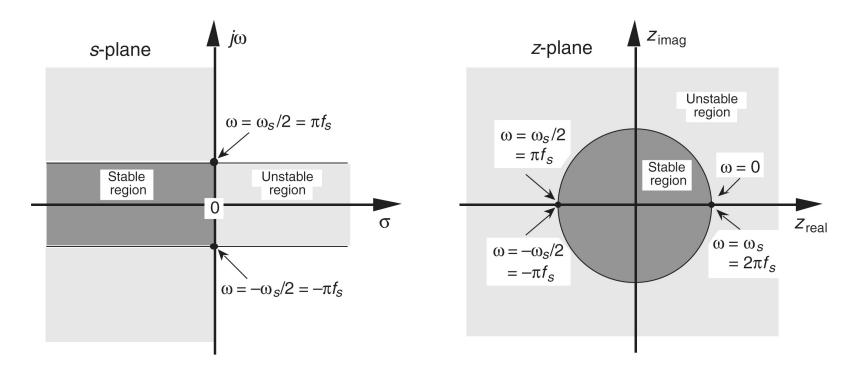


Figure 6-12 The Laplace *s*-*p*lane showing the regions of stability and instability for pole locations for linear continuous systems.



**Figure 6-13** Unit circle on the complex *z*-plane.



**Figure 6-14** Mapping of the Laplace *s*-plane to the *z*-plane. All frequency values are in radians/second.

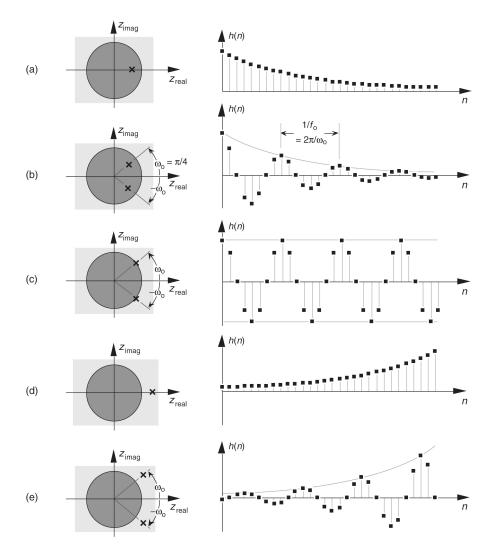
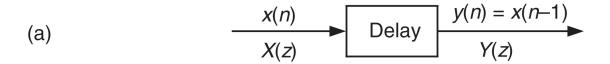
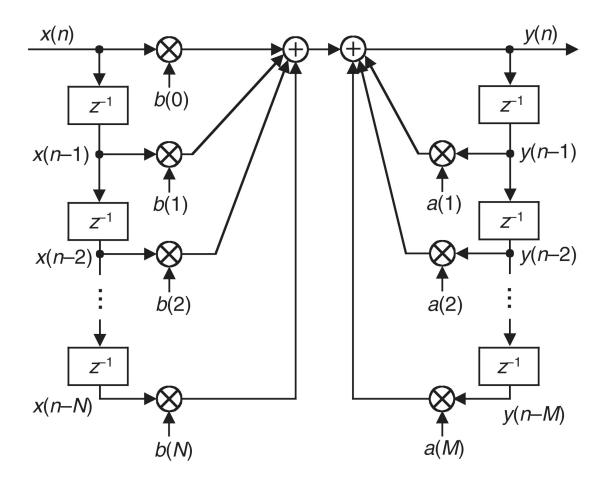


Figure 6-15 Various *H*(*z*) pole locations and their discrete time-domain impulse responses: (a) single pole inside the unit circle; (b) conjugate poles located inside the unit circle; (c) conjugate poles located on the unit circle; (d) single pole outside the unit circle; (e) conjugate poles located outside the unit circle.



**Figure 6-16** Time- and z-domain delay element relationships: (a) single delay; (b) multiple delays.



**Figure 6-17** General (Direct Form I) structure of an Mth-order IIR filter, having N feedforward stages and M feedback stages, with the  $z^{-1}$  operator indicating a unit time delay.

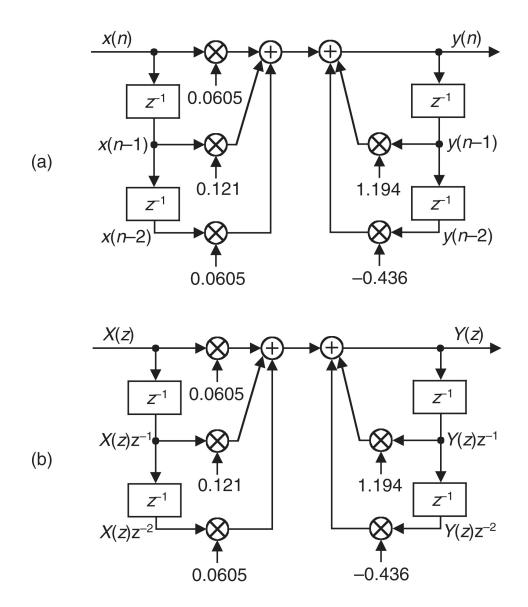
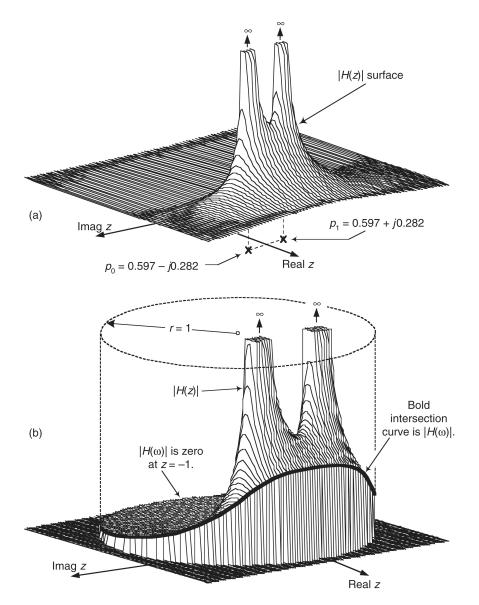
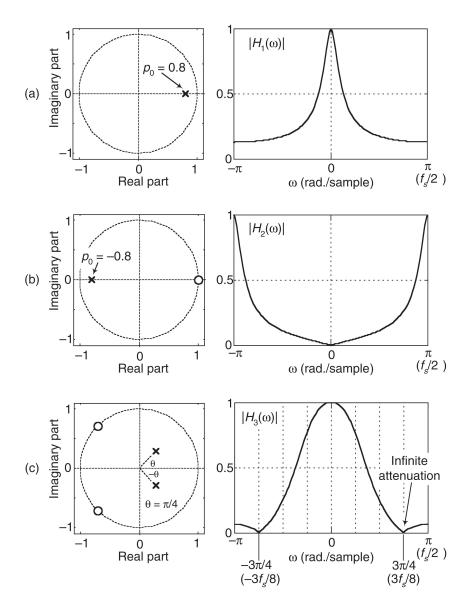


Figure 6-18 Second-order lowpass IIR filter example.



**Figure 6-20** IIR filter's |H(z)| surface: (a) pole locations; (b) frequency magnitude response.



**Figure 6-21** IIR filter poles/zeros and normalized frequency magnitude responses.